

$$(2) \quad 3.3-1, \quad T = \frac{3As^2}{v}, \quad P = \frac{As^3}{v^2}$$

(a) Find μ as a function of S, v , then find the fundamental eq.

By Gibbs-Duhem Relation, $du = vdp - sdT$

$$dp = d\left(\frac{As^3}{v^2}\right)$$

$$dT = d\left(\frac{3As^2}{v}\right)$$

$$= \frac{3As^2}{v^2} ds - \frac{2As^3}{v^3} dv$$

$$= \frac{6As}{v} ds - \frac{3As^2}{v^2} dv$$

$$\Rightarrow du = vdp - sdT$$

$$= \frac{3As^2}{v} ds - \frac{2As^3}{v^2} dv - \frac{6As^2}{v} ds + \frac{3As^3}{v^2} dv$$

$$= -\frac{3As^2}{v} ds + \frac{As^3}{v^2} dv$$

integrating yields $\mu(s, v) = -\frac{As^3}{v} + -\frac{As^3}{v}$

$$= \boxed{-\frac{2As^3}{v} + C}$$

Then Euler Eq. states $U = TS - PV + \mu N$

$$= NT_s - NP_v + \mu N$$

$$= N \left[\frac{3As^3}{v} - \frac{As^3}{v} \right] - \frac{N \cdot 2As^3}{v}$$

$$\boxed{= 0} \quad ?$$

(b) Find the fundamental equation of this system by direct integration.

$$du = Tds - PdV$$

$$\Rightarrow \left(u = \frac{2AS^3}{V} \right)$$